Lecture 5: Intermediate macroeconomics, autumn 2008 Lars Calmfors

#### Purchasing power parity – PPP

- Theory of determination of the exchange rate in the long run, which emphasises the importance of goods markets (in contrast to asset markets)
- **Gustaf Cassel (1866 1945)**

#### Law of one price

 $P_{US}^i = E_{\text{s}} e^{g} P_E^i$  $E_{\text{s}} = P_{US}^i / P_E^i$ 

#### Absolute purchasing power parity

 $E_{\rm S/E} = P_{US} \ / \ P_{E}$ 

#### **Relative purchasing power parity**

$$(E_{\text{S/}\notin t} - E_{\text{S/}\notin t-1}) / E_{\text{S/}\notin t-1} = \pi_{US, t} - \pi_{E, t}$$
$$\pi_t = (P_t - P_{t-1}) / P_{t-1}$$

# Fig. 15-2: The Yen/Dollar Exchange Rate and Relative Japan-U.S. Price Levels, 1980–2006



Source: IMF, International Financial Statistics. Exchange rates and price levels are end-of-year data.

#### **Causes of deviations from PPP**

- 1. Transport costs and trade barriers
- 2. Differences in consumption baskets
- 3. Imperfect competition price discrimination pricing to market

## <u>Different PPP exchange rates depending on which country's</u> <u>consumption basket is used</u>

 $P_{US}/P_G$  is higher with German basket than with US basket, because goods that are relatively cheap in the US have a larger weight in the American than in the German basket.

#### **Different types of goods and services**

- Tradables or traded goods
- Non-tradables or non-traded goods (primarily services and building)





a) The exchange rate is based on monthly data, while PPPs are given at an annual frequency. Different PPPs are computed with respect to the different consumption baskets in the United States, the OECD and Germany. See footnote 8, Chapter 1, EEAG (2005).

Sources: European Central Bank, Federal Statistical Office, OECD and calculations by the Ifo Institute.

**EEAG Report 2008** 

#### The Balassa-Samuelson-effect

The price level is higher in countries with high per capita income, because prices of non-tradables are higher.

- (1)  $P_T = EP_T^*$  (international goods arbitrage)
- (2)  $W_T = P_T \cdot MPL_T$  (profit maximisation in tradables sector)

for

(3)  $W_N = W_T$  (homogenous labour market)

(4) 
$$P_N = W_N / MPL_N$$
 (price = marginal cost  
non-tradables)

(5) 
$$P_C = P_T^{\alpha} P_N^{1-\alpha}$$
 (consumer price index)

<u>The Balassa-Samuelson effect implies a higher relative price for</u> <u>non-tradables in rich than in poor countries:</u>

$$\frac{P_N}{P_T} = \frac{1}{P_T} \cdot \frac{W_N}{MPL_N} = \frac{1}{P_T} \cdot \frac{W_T}{MPL_N} = \frac{P_T \cdot MPL_T}{P_T \cdot MPL_N} = \frac{MPL_T}{MPL_N}$$
$$\frac{MPL_T}{MPL_N} \uparrow \implies \frac{P_N}{P_T} \uparrow$$

- Compare countries with the same currency (for example countries in the euro area)
- $P_T$  is the same everywhere because of goods arbitrage
- *MPL<sub>T</sub>* is higher in rich than in poor countries (more real and human capital gives higher productivity).
- Higher  $MPL_T$  implies higher  $W_T = P_T \cdot MPL_T$ .
- A homogenous labour market implies  $W_N = W_T$
- Differences in *MPL<sub>N</sub>* (the marginal product of labour in the non-tradables sector) between countries are small (a hair cut takes more or less the same time everywhere)
- Because  $P_N = W_N / MPL_N$ , the price level for non-tradables must be higher in rich than in poor countries
- Hence  $P_C$  (CPI) must be higher.

# Fig. 15-3: Price Levels and Real Incomes, 2004

Price level relative to U.S. (U.S. = 100)



- According to the catching-up hypothesis growth is higher in poor than in rich countries
- The main difference in growth is higher productivity growth in the tradables sector (manufacturing)
- Poor countries with high growth tend to have higher inflation that rich: with a common currency (fixed exchange rates), Estonia and Latvia will have higher inflation than Germany.

## Higher inflation in poor than in rich countries

$$(1) \quad \frac{\Delta P_T}{P_T} = \frac{\Delta E}{E} + \frac{\Delta P_T}{P_T}$$

$$(2) \quad \frac{\Delta W_T}{W_T} = \frac{\Delta P_T}{P_T} + \frac{\Delta M P L_T}{M P L_T}$$

$$(3) \quad \frac{\Delta W_N}{W_N} = \frac{\Delta W_T}{W_T}$$

$$(4) \quad \frac{\Delta P_N}{P_N} = \frac{\Delta W_N}{W_N} - \frac{\Delta M P L_N}{M P L_N}$$

$$(5) \quad \frac{\Delta P_C}{P_C} = \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \frac{\Delta P_N}{P_N} = \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta W_N}{W_N} - \frac{\Delta M P L_N}{M P L_N} \right\} =$$

$$= \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta W_T}{W_T} - \frac{\Delta M P L_N}{M P L_N} \right\} = \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta P_T}{M P L_T} - \frac{\Delta M P L_N}{M P L_N} \right\} =$$

$$= \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta M P L_T}{M P L_T} - \frac{\Delta M P L_N}{M P L_N} \right\}$$

#### Arithmetical illustration of Balassa-Samuelson effect

$$\frac{\Delta P_T}{P_T} = 0$$
$$\frac{\Delta MPL_N}{MPL_N} = 1\%$$
$$\alpha = 0.5$$

### <u>Estonia</u>

$$\frac{\Delta MPL_T}{MPL_T} = 8 \%$$

$$\frac{\Delta P_C}{P_C} = \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta MPL_T}{MPL_T} - \frac{\Delta MPL_N}{MPL_N} \right\} = 0 + 0.5 (8-1) = 3.5 \%$$

#### **Germany**

$$\frac{\Delta MPL_T}{MPL_T} = 4 \%$$

$$\frac{\Delta P_C}{P_C} = \alpha \frac{\Delta P_T}{P_T} + (1 - \alpha) \left\{ \frac{\Delta MPL_T}{MPL_T} - \frac{\Delta MPL_N}{MPL_N} \right\} = 0 + 0.5 (4-1) = 1.5 \%$$

• Inflation should be about 2 percentage points higher in Estonia than in Germany because of higher growth.

### The monetary approach to the exchange rate

$$E = P_{US} / P_E$$
$$P_{US} = M_{US}^S / L (R_{\$}, Y_{US})$$
$$P_E = M_E^S / L (R_{\clubsuit}, Y_E)$$

### The fundamental exchange rate equation

$$E = P_{US} / P_E = (M_{US}^S / M_E^S) \bullet [L(R_{\notin}, Y_E) / L(R_{\$}, Y_{US})]$$

An increase in money supply in the US relative to Europe  $(M_{US}^S / M_E^S \uparrow)$  causes a nominal depreciation of the dollar  $(E\uparrow)$ .

### **The Fisher effect**

(1) 
$$R_{\$} = R_{€} + (E^e - E) / E$$
 Interest rate parity

(2) 
$$\frac{E^e - E}{E} = \pi^e_{US} - \pi^e_E$$
 Relative PPP

Substitution of (2) in (1):

$$R_{\$} - R_{€} = \pi_{US}^e - \pi_E^e$$

<u>The Fisher effect</u>: a 1 percentage point rise in inflation in one country causes a 1 percentage point increase in the nominal interest rate.





#### Real and nominal exchange rates

 $q = EP_E/P_{US}$ 

- With a flexible nominal exchange rate, the real exchange rate can change both because the nominal exchange rate (E) and the relative price in national currencies  $(P_E/P_{US})$  change.
- In a currency union (or with a fixed nominal exchange) rate the real exchange rate can change only through a change in the relative price in national currencies
- If output/employment in the long run increase in the US relative to Europe, the relative price of American goods must fall if these are to be sold, i.e. there must be a real depreciation for the US.

The real exchange rate equation can be rearranged:

 $E = q \cdot P_{US}/P_E$ 

The nominal exchange rate (*E*) can change either because the relative price level in national currencies between the countries ( $P_E/P_{US}$ ) changes or because the real exchange rate (*q*) changes.

# Determining the Long Run Real Exchange Rate (cont.)

The demand for US products relative to the demand for EU products depends on the relative price of these products, or the real exchange rate. When the real exchange rate,  $q_{US/EU} = (E_{s/e}P_{EU})/P_{US}$ is high, the relative demand for US products is high.



The long-run equilibrium real exchange rate equates world relative demand to the fullemployment level of relative supply.

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#### Interest rate differentials and real exchange rate changes

 $q = EP_E / P_{US}$  Definition of real exchange rate (1)  $(q^e - q) / q = (E^e - E) / E + \pi_E^e - \pi_{US}^e$ (2)  $(E^e - E) / E = R_{s} - R_{\epsilon}$  Interest rate parity

Substitution of (2) into (1):

$$(q^{e} - q) / q = R_{s} - R_{e} + \pi_{E}^{e} - \pi_{US}^{e}$$
  
 $R_{s} - R_{e} = \pi_{US}^{e} - \pi_{E}^{e} + (q^{e} - q) / q$ 

Nominal interest rate differential = inflation differential + real depreciation

$$(R_{s} - \pi_{US}^{e}) - (R_{e} - \pi_{E}^{e}) = (q^{e} - q) / q$$
  
 $r_{US}^{e} - r_{E}^{e} = (q^{e} - q) / q$ 

*r* = real interest rate

Real interest rate differential = real depreciation (real interest rate parity)

## <u>A short-run general equilibrium model for an open economy</u> <u>with a flexible exchange rate</u>

#### Aggregate demand for domestically produced goods

D = C + G + I + CA

C = C(Y - T)	Consumption function			
$G = \overline{G}$	Exogenous government expenditure			
$T = \overline{T}$	Exogenous lump-sum tax			
$I = \overline{I}$	Exogenous investment			
CA = EX - IM = EX -	IM			

The current account (net exports) should be measured in terms of the same numéraire (here domestic goods). So *IM* is imports measured in terms of domestic goods. *IM*\* is imports measured in terms of foreign goods.

$$EX = EX(q, Y^*)$$
  

$$IM^* = IM^*(q, Y - T)$$
  

$$CA = EX(q, Y^*) - qIM^*(q, Y - T) = CA(q, Y^*, Y - T)$$

A real depreciation  $(q\uparrow)$  need not improve the current account  $(CA\uparrow)$ . <u>Volume effects</u> on exports and imports work in this direction, but the <u>value effect</u> on imports works in the reverse direction.

#### **Marshall-Lerner condition**

A real depreciation will increase net exports if the Marshall-Lerner condition holds.

The price elasticity of exports + the price elasticity of imports > 1

Then the volume effects dominate the value effect for imports.

All elasticities are defined to be positive.

#### **Mathematical derivation**

$$CA(q, Y^*, Y-T) = EX(q, Y^*) - qIM^*(q, Y-T)$$

#### Rule of differentiation for a product

$$\frac{d\left[v(x)u(x)\right]}{dx} = v_x(x)u(x) + u_x(x)v(x)$$

A real depreciation  $(q\uparrow)$  improves the current account  $(CA\uparrow)$ if  $dCA/dq = CA_q > 0$ .

$$\frac{dCA}{dq} = EX_q - qIM_q^* - IM^*$$

Multiply the equation by *q/EX*.

$$\frac{q}{EX} \cdot \frac{dCA}{dq} = \frac{qEX_q}{EX} - \frac{q^2IM_q^*}{EX} - \frac{qIM^*}{EX}$$

Assume that CA = 0 initially, so that  $EX = qIM^* = IM$ .

$$\frac{q}{EX} \cdot \frac{dCA}{dq} = \frac{qEX_q}{EX} - \frac{qIM_q^*}{IM^*} - 1$$

$$\frac{dCA}{dq} > 0 \iff \frac{qEX_q}{EX} - \frac{qIM_q^*}{IM^*} > 1$$

$$\frac{qEX_q}{EX} = \frac{q}{EX} \cdot \frac{\partial EX}{\partial q} = \eta = \text{price elasticity of exports}$$
$$-\frac{qIM_q^*}{IM^*} = -\frac{q}{IM^*} \cdot \frac{\partial IM^*}{\partial q} = \eta^* = \text{price elasticity of imports}$$

All price elasticities have been defined so that they are positive.  $\therefore \eta + \eta * > 1 \Leftrightarrow dCA/dq > 0.$ 



TABLE 16A2-1	1 Estimated Price Elasticities for International Trade in Manufactured Goods						
	η		$\eta^*$				
Country	Impact	Short-run	Long-run	Impact	Short-run	Long-run	
Austria	0.39	0.71	1.37	0.03	0.36	0.80	
Belgium	0.18	0.59	1.55		—	0.70	
Britain	—	—	0.31	0.60	0.75	0.75	
Canada	0.08	0.40	0.71	0.72	0.72	0.72	
Denmark	0.82	1.13	1.13	0.55	0.93	1.14	
France	0.20	0.48	1.25		0.49	0.60	
Germany		_	1.41	0.57	0.77	0.77	
Italy		0.56	0.64	0.94	0.94	0.94	
Japan	0.59	1.01	1.61	0.16	0.72	0.97	
Netherlands	0.24	0.49	0.89	0.71	1.22	1.22	
Norway	0.40	0.74	1.49	_	0.01	0.71	
Sweden	0.27	0.73	1.59			0.94	
Switzerland	0.28	0.42	0.73	0.25	0.25	0.25	
United States	0.18	0.48	1.67	_	1.06	1.06	

**Note:** Estimates are taken from Jacques R. Artus and Malcolm D. Knight, *Issues in the Assessment of the Exchange Rates of Industrial Countries.* Occasional Paper 29. Washington, D.C.: International Monetary Fund, July 1984, table 4. Unavailable estimates are indicated by dashes.

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Source: International Monetary Fund, International Financial Statistics.

# Value Effect, Volume Effect and the J-Curve (cont.)



$$D = C(Y - T) + G + I + CA(EP^*/P, Y^*, Y - T)$$
$$D = D(EP^*/P, Y - T, G, I, Y^*)$$

$$EP^*/P^{\uparrow} \Rightarrow D^{\uparrow}$$
$$(Y - T)^{\uparrow} \Rightarrow D^{\uparrow}$$
$$G^{\uparrow} \Rightarrow D^{\uparrow}$$
$$I^{\uparrow} \Rightarrow D^{\uparrow}$$
$$Y^*^{\uparrow} \Rightarrow D^{\uparrow}$$



#### Figure 16-1

#### Aggregate Demand as a Function of Output

Aggregate demand is a function of the real exchange rate (EP\*/P), disposable income (Y-T), investment demand (I), and government spending (G). If all other factors remain unchanged, a rise in output (real income), Y, increases aggregate demand. Because the increase in aggregate demand is less than the increase in output, the slope of the aggregate demand function is less than 1 (as indicated by its position within the 45-degree angle).



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# Short Run Equilibrium for Aggregate Demand and Output (cont.)



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# Short Run Equilibrium and the Exchange Rate: *DD* Schedule (cont.)



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Short Run Equilibrium and the Exchange Rate: *DD* Schedule (cont.)





# Shifting the *DD* Curve (cont.)



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#### Changes shifting the DD-curve to the right

- **1.** An increase in government expenditure  $(G\uparrow)$
- **2.** A reduction in the tax  $(T\downarrow)$
- 3. An increase in investment  $(I^{\uparrow})$
- 4. A reduction in the domestic price level  $(P\downarrow)$
- 5. An increase in the foreign price level  $(P^*\uparrow)$
- 6. An increase in foreign income  $(Y^*\uparrow)$
- 7. A reduction in the savings rate  $(s\downarrow)$
- 8. A shift in expenditure from foreign to domestic goods (increased relative demand for domestic goods)

## Equilibrium in asset markets

1. Foreign currency market (interest rate parity)  $R = R^* + (E^e - E)/E$ 

2. Money market  $M^{s}/P = L(R, Y)$ 



# Short Run Equilibrium for Assets (cont.)



#### Figure 16-6

#### Output and the Exchange Rate in Asset Market Equilibrium

For the asset (foreign exchange and money) markets to remain in equilibrium, a rise in output must be accompanied by an appreciation of the currency, all else equal.

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## Short Run Equilibrium for Assets: *AA* Curve (cont.)



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### **Factors shifting the AA-curve upwards**

- 1. An increase in money supply  $(M^{s\uparrow})$
- **2.** A reduction in the price level  $(P\downarrow)$
- 3. An expected future depreciation  $(E^{e}\uparrow)$
- 4. A higher foreign interest rate  $(R^*\downarrow)$
- 5. A reduction in domestic money demand

## AN INCREASE IN MONEY SUPPLY, A REDUCTION OF THE PRICE LEVEL



# AN EXPECTED DEPRECIATION, AN INCREASE IN THE FOREIGN INTEREST RATE





## Putting the Pieces Together: the DD and AA Curves (cont.)

#### Figure 16-8

## Short-Run Equilibrium: The Intersection of *DD* and *AA*

The short-run equilibrium of the economy occurs at point 1, where the output market (whose equilibrium points are summarized by the *DD* curve) and asset market (whose equilibrium points are summarized by the *AA* curve) simultaneously clear.



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## How the Economy Reaches Equilibrium in the Short Run





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### **Temporary Changes** in Monetary Policy (cont.) Figure 16-10 Exchange rate, E Effects of a Temporary Increase in the Money Supply DD By shifting $AA^1$ upward, a temporary increase in the money supply causes a currency depreciation and a rise in output. 2 $E^2$ $E^1$ $AA^1$ $\gamma^2$ $Y^1$ Output, Y

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AA<sup>2</sup>



# **Temporary Changes** in Fiscal Policy (cont.)

Figure 16-11

Expansion

output.



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# Policies to Maintain Full Employment (cont.)



#### **Problems with stabilisation policy**

- Policies can easily become too expansionary on average ("inflation bias")
- It is difficult *ex ante* to identify disturbances and how strong they are
- An expansionary fiscal policy can cause permanent budget deficits
- "Decision lags"



## Effects of Permanent Changes in Monetary Policy in the Short Run

#### Figure 16-14

Short-Run Effects of a Permanent Increase in the Money Supply A permanent increase in the money supply, which shifts AA<sup>1</sup> to AA<sup>2</sup> and moves the economy from point 1 to point 2, has stronger effects on the exchange rate and output than an equal temporary increase, which moves the economy only to point 3.



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## Effects of Permanent Changes in Monetary Policy in the Long Run (cont.)



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# Effects of Permanent Changes in Fiscal Policy (cont.)

#### Figure 16-16

#### Effects of a Permanent Fiscal Expansion

Because a permanent fiscal expansion changes exchange rate expectations, it shifts  $AA^1$  leftward as it shifts  $DD^1$  to the right. The effect on output (point 2) is nil if the economy starts in long-run equilibrium. A comparable *temporary* fiscal expansion, in contrast, would leave the economy at point 3.



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#### Why has a permanent fiscal policy no output effects?

- 1. In the long run we have  $Y = Y_f$  och  $R = R^*$  (output and interest rate at their equilibrium levels). Because  $P = M^{s}/L(Y_f, R^*,) P$  must be unchanged in the long run.
- 2. In the short run M<sup>s</sup>/P is given. Assume that Y↑. Then R↑.
  From interest rate parity we then have (E<sup>e</sup> E) ↑.
  A nominal exchange rate depreciation is expected.
- 3. But an expected nominal depreciation must also imply an expected real depreciation as P is given in the long run. This cannot be true because Y must then increase even more in the long run than in the short run and can then never return to its equilibrium level  $Y_{f.}$
- 4. But everything will fit together if Y never changes, so that  $Y = Y_f$  even in the short run.

The mathematics of a permanent fiscal expansion

$$\frac{M^s}{P} = L(Y, R) \tag{1}$$

$$R = R^* + (E^e - E)/E$$
 (2)

$$Y = D(EP*/P, Y-T, I, G, Y*)$$
 (3)

If  $\uparrow \Rightarrow E = E^e \downarrow$  so that *Y* remains constant according to equation (3), equations (1) and (2) are also fulfilled.

#### **Further aspects on exchange rates**

- The current account and the exchange rate
- Investors might start to question US ability to service debt (cumulated current account deficits)
- Capital inflows to the US could stop and capital flows could even be reversed: unless the current account deficits are offset by capital inflows there will be an excess supply of dollars and the dollar must depreciate.
- But US assets abroad are mostly denominated in foreign currency, whereas debt is in dollars, so a depreciation of the dollar will reduce US net debt to the rest of the world
- Hence no risk that the value effects of a dollar depreciation would lead to a financial crisis because net foreign debt would increase (as has happened in many emerging economies